

# A Fiscal Theory of Sovereign Risk

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## Question

- ▶ How does monetary policy regime impact stochastic process for default on government debt when fiscal policy does not act to stabilize debt?
  - ▶ Monetary Regimes: Taylor Rules, Price Level targeting
  - ▶ Tension between price stability and government solvency depending on monetary regime
  - ▶ Small differences in monetary policy specification can imply large differences in default outcomes

# Approach

- ▶ To ensure government PVBC holds, typically assume either fiscal or monetary policy is passive
  - ▶ Fiscal Policy - Passive if adjust primary surplus to ensure solvency
  - ▶ Monetary Policy - Active if reacts sufficiently strongly to inflation (Taylor Principle)
- ▶ This Paper - Assumes Fiscal Policy is Active (primary surplus set exogenously), and Monetary Policy is Active
  - ▶ To ensure solvency, government may have to default on portion of (nominal) liabilities

# Model

- ▶ Constant Endowment  $y$ , (real) lump sum taxes  $\tau_t$ , identical households
- ▶ Assets - Complete Markets ( $D_t$  - Arrow Securities), (Risky) Government Debt  $B_t$  with default rate  $\delta_t$
- ▶  $\max \mathbb{E}_t \sum_{t=0}^{\infty} \beta^t U(C_t)$ 
  - ▶ s.t.  $P_t C_t + \mathbb{E}_t m_{t+1} D_{t+1} + B_t + P_t \tau_t \leq D_t + P_t y + B_{t-1} R_{t-1} (1 - \delta_t)$
- ▶ Where  $\tau_t - \bar{\tau} = \rho(\tau_{t-1} - \bar{\tau}) + \epsilon_t$ , with  $\epsilon_t \sim N(0, \sigma^2)$
- ▶ Gov't BC:  $B_t = R_{t-1} B_{t-1} (1 - \delta_t) - \tau_t P_t$
- ▶ Euler:  $\beta R_t \mathbb{E}_t (1 - \delta_{t+1}) \frac{P_t}{P_{t+1}} = 1$
- ▶ Goal: Characterize  $\delta_t$  given monetary policy stance

# Default Process

- ▶ Iterate forward on Government Flow BC:
- ▶ 
$$\delta_t = 1 - \frac{\sum_{h=0}^{\infty} \beta^h \mathbb{E}_t \tau_{t+h}}{R_{t-1} B_{t-1} / P_t}$$
- ▶ Government defaults to extent present value of primary surpluses falls short of initial government liabilities
  - ▶ If  $\delta_t = 0$ , obtain Fiscal Theory of Price Level Determination
- ▶ 
$$\delta_t = 1 - \frac{(1-\beta)(\tau_t - \bar{\tau}) + (1-\beta\rho)\tau}{R_{t-1} B_{t-1} / P_{t-1} (1-\beta)(1-\beta\rho)}$$
 (Given  $\tau_t \sim \text{AR}(1)$ )
  - ▶ More persistent tax processes imply larger default on public debt for given decline in current tax revenues
- ▶ Equilibrium Characterization requires  $P_t$  law of motion - need to specify monetary policy

## Solution - Contemporaneous Taylor Rule

- ▶  $R_t = \frac{\pi^*}{\beta} + \alpha \left( \frac{P_t}{P_{t-1}} - \pi^* \right)$ , MP active ( $\alpha\beta > 1$ )
- ▶ CB cannot achieve inflation target without defaulting:
  - ▶  $\delta_0 = 0$  implies  $P_0 = \frac{R_{-1}B_{-1}}{\sum_{h=0}^{\infty} \beta^h \mathbb{E}_0 \tau_h}$
  - ▶  $\frac{P_0}{P_{-1}}$  will thus differ from target
- ▶ Taylor Rule + Euler Equation imply  $\pi_{t+1} = \alpha\beta\pi_t + (1 - \alpha\beta)\pi^*$ 
  - ▶ Eventual hyperinflation/hyperdeflation

## Solution - Contemporaneous Taylor Rule

- ▶ CB can achieve inflation target in every period if default occurs:
  - ▶  $\delta_0 = 1 - \frac{\pi^* \sum_{h=0}^{\infty} \beta^h \mathbb{E}_0 \tau_h}{R_{-1} B_{-1} / P_{-1}}$
  - ▶  $\delta_t = 1 - \frac{\sum_{h=0}^{\infty} \beta^h \mathbb{E}_t \tau_h}{\sum_{h=0}^{\infty} \beta^h \mathbb{E}_{t-1} \tau_h}, t \geq 1$
  - ▶ Default occurs in proportion to innovations in expectations to PV surpluses
- ▶ Default rate unforecastable:  $\mathbb{E}_t \delta_{t+1} = 0$  for all  $t$

## Contemporaneous Taylor Rule - Delaying Default

- ▶ Delaying Default counterproductive if MP follows contemporaneous Taylor Rule
- ▶ Assume perfect foresight,  $\pi_0 > \pi^*$ ,  $\tau_t = \bar{\tau}$
- ▶ Fiscal Authority sets  $\delta_t = 0$ , for  $0 \leq t < T$
- ▶ Period T set default rate to ensure inflation target met (thereafter no default)
- ▶  $\pi_t = \pi^* + (\alpha\beta)^t(\pi_0 - \pi^*)$ , for  $0 \leq t < T - 1$
- ▶ In period T default rate:  $\delta_T = 1 - \frac{\pi^*}{\pi^* + (\alpha\beta)^T(\pi_0 - \pi^*)}$ 
  - ▶ Longer default delayed - Higher inflation rate, higher default rate required to stabilize prices



## Solution - Forward Looking Taylor Rule

- ▶  $R_t = \frac{\pi^*}{\beta} + \alpha \left( \frac{1}{\mathbb{E}_t P_t / P_{t+1}} - \pi^* \right)$  MP active ( $\alpha\beta > 1$ )
- ▶ CB can anchor expected inflation at target with no default:
  - ▶  $\frac{1}{\mathbb{E}_t P_t / P_{t+1}} = \pi^*$ ,  $\delta_t = 0$  for all t
  - ▶  $\frac{P_t}{P_{t-1}} = \pi^* \frac{\sum_{h=0}^{\infty} \beta^h \mathbb{E}_{t-1} \tau_h}{\sum_{h=0}^{\infty} \beta^h \mathbb{E}_t \tau_h}$
  - ▶ Unexpected innovations in inflation absorb shocks to PV of primary surpluses

## Solution - Price Level Targeting

- ▶ Now suppose MP strictly targets price level:  $P_t = 1 \quad \forall t$
- ▶ Government loses ability to inflate away real value of liabilities
  - ▶ Since fiscal policy is exogenous, default will occur in equilibrium
- ▶ 
$$\delta_t = 1 - \frac{(1-\beta)(\tau_t - \bar{\tau}) + (1-\beta\rho)\bar{\tau}}{R_{t-1}B_{t-1}(1-\beta)(1-\beta\rho)}$$
- ▶ 
$$B_t = 1 - \frac{\beta\rho(1-\beta)(\tau_t - \bar{\tau}) + \beta(1-\beta\rho)\bar{\tau}}{(1-\beta)(1-\beta\rho)}$$
  - ▶ More persistent tax process implies greater fall in debt for given fall in tax revenue

## Solution - Price Level Targeting

- ▶ Solve for default process under three default rules:

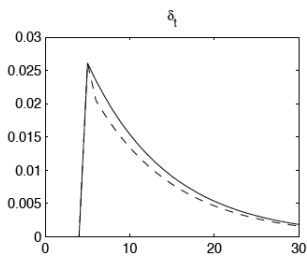
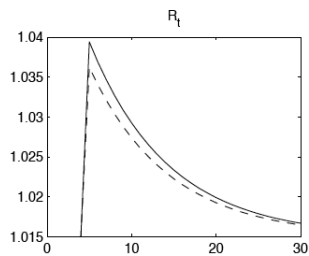
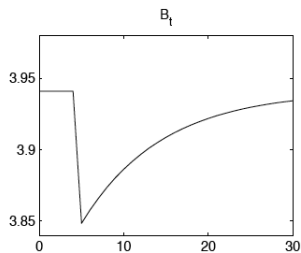
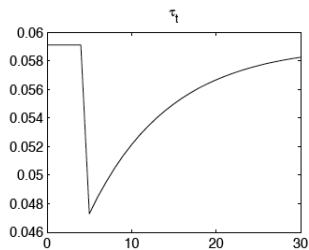
- ▶ Rule 1 -  $\delta_t = \begin{cases} > 0 & \text{if } \frac{\tau_t}{B_{t-1}} < \gamma \\ 0 & \text{if } \frac{\tau_t}{B_{t-1}} = \gamma \\ < 0 & \text{if } \frac{\tau_t}{B_{t-1}} > \gamma \end{cases}$

- ▶ Rule 2 -  $\delta_t = \begin{cases} > 0 & \text{if } \frac{\tau_t}{y} < \gamma \\ 0 & \text{if } \frac{\tau_t}{y} = \gamma \\ < 0 & \text{if } \frac{\tau_t}{y} > \gamma \end{cases}$

- ▶ Rule 3 - Interest Rate Targeting:  $R_t = \beta^{-1}$

- ▶ Calibration - Real Interest Rate 6%, Debt/GDP ratio 100%,  $\rho = 0.9$ ,  $\gamma$  chosen so that in steady-state government does not default
- ▶ Negative shock to tax revenues (20% below average)

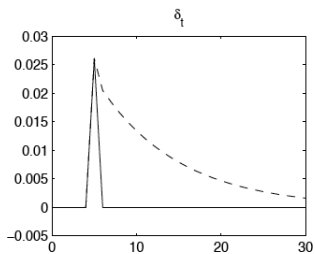
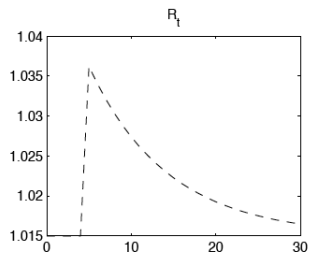
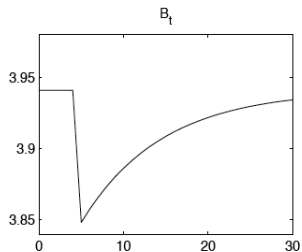
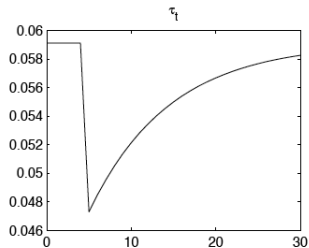
## Solution - Price Level Targeting Rule 1 and 2



— Default Rule 2

- - - Default Rule 1

# Solution - Price Level Targeting Rule 1 and 3



— Interest Rate Peg

- - - Default Rule 1

# Solution - Price Level Targeting

- ▶ Rules reacting to Taxes/Debt or Taxes/GDP: default rate persistent, very similar dynamics
  - ▶ Default rate larger if stabilize Taxes/GDP - Debt falls in response to drop in tax revenue, while output is exogenous
- ▶ Interest rate targeting:  $\mathbb{E}_t \delta_{t+1} = 0$ 
  - ▶ Cumulative default much lower under interest rate targeting - lower debt burden because of lower interest rate